

1 **Calibration of a Mechanistic-Empirical Fatigue Model under Different Moisture Conditions**

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**1 ABSTRACT**

2 Traditionally, the design of pavements in Central America has been made using the AASHTO 93  
3 design method, which is based on empirical correlations from results obtained several decades ago  
4 in the AASHO road test. To return to the use of more fundamental engineering principles, the  
5 necessity of a transition from this empirical state to a mechanistic-empirical one has been  
6 recognized. The National Laboratory of Materials and Structural Models of the University of  
7 Costa Rica (LanammeUCR) has implemented an Accelerated Pavement Testing (APT) program,  
8 and; a Heavy Vehicle Simulator (HVS) provides a first step in the validation/calibration process of  
9 fatigue and deformation models.

10 In addition, the effect of moisture is fundamental in determining pavement responses. The effect  
11 becomes more important when high levels of moisture and precipitation are present that is the case  
12 of tropical regions such as Central America where high precipitation rates, high variability in water  
13 table levels, and materials highly susceptible to the previous are common.

14 Consequently, to capture the effect of moisture on pavement performance, 4 APT tests have been  
15 conducted to compare how a pavement section deteriorates in the presence of water: pavement  
16 sections were initially evaluated under optimum moisture conditions and replicas of the sections  
17 were later evaluated under high water table conditions and surface precipitation. These sections are  
18 used to calibrate 4 different fatigue damage models.

19

20 *Keywords:* Damage, Fatigue, Pavement performance, Moisture

## 1 INTRODUCTION

2 Important progress in pavement engineering have been traditionally achieved through real time  
3 load (RTL) testing because the technique does not require large specialized equipment for carrying  
4 out the tests (1, 2). However, the time required to perform the RLT tests (more than 10 years of  
5 continuous monitoring of an experimental section) is associated with many difficulties since most  
6 of the experimental sections are located along roadways in operation.

7 In the case of Central America, the big variability in materials, traffic, climatic  
8 conditions, and the cost of developing a suitable RTL test program covering all these conditions is  
9 prohibitive. Due to local conditions, there is a great need to characterize the performance of local  
10 pavement structures as the only means of developing and calibrating design methodologies. For  
11 this purpose, it was considered that the implementation of an Accelerated Pavement Testing (APT)  
12 program was a better alternative (3).

13 High loads traveling at low speeds, expansive soils and drainage systems that are  
14 insufficient or non-existent to meet the demand of the rainy season are common in the region. All  
15 the previous factors combine to generate high moisture damage probability that can range from  
16 stripping of the asphalt film, batches and cracking that allow water to enter the pavement structure,  
17 and changes in material response due to moisture dependent behavior of the unbound layers; all  
18 leading to an overall structural and functional failure of the pavement structure.

19 The effect of moisture on the different materials used in pavement construction has been analyzed  
20 by several authors, but the calibration of pavement response models that consider this effect are  
21 highly dependent on the material and climatic conditions for each region.

22 To attend this need, a Costa Rican APT program was implemented (PaveLab), relying on  
23 a Heavy Vehicle Simulator (HVS) since it was considered the best option for the local and regional  
24 needs. Specifically, the PaveLab had to meet the following requirements: mobility, accelerated  
25 pavement evaluation, application of real loads and comparable results to similar equipment (4, 5,  
26 6). To evaluate the effect of moisture on pavement performance, pavement structures with  
27 different types of base and under different humidity conditions in the lower layers have been  
28 analyzed. With the current project, PaveLab aims to generate a series of products that have already  
29 been obtained under similar studies but for different conditions (7, 8, 9):

- 30 • Mechanistic-empirical pavement design methodology and software based on material  
31 conditions, weather, traffic and actual construction practices.
- 32 • Development of new material specifications that are based on actual performance and  
33 contribution of structural materials in the field.
- 34 • Optimization of pavement structures in use at the national level, based on structural, materials,  
35 traffic, and climatic conditions specific to the area where the structure is planned to be built.
- 36 • Potential for an improved evaluation methodology of new materials or materials currently in  
37 use.
- 38 • Capacity to evaluate pavement structures of high importance prior to opening to traffic to  
39 ensure the required performance of the structure or identify possible deficiencies.

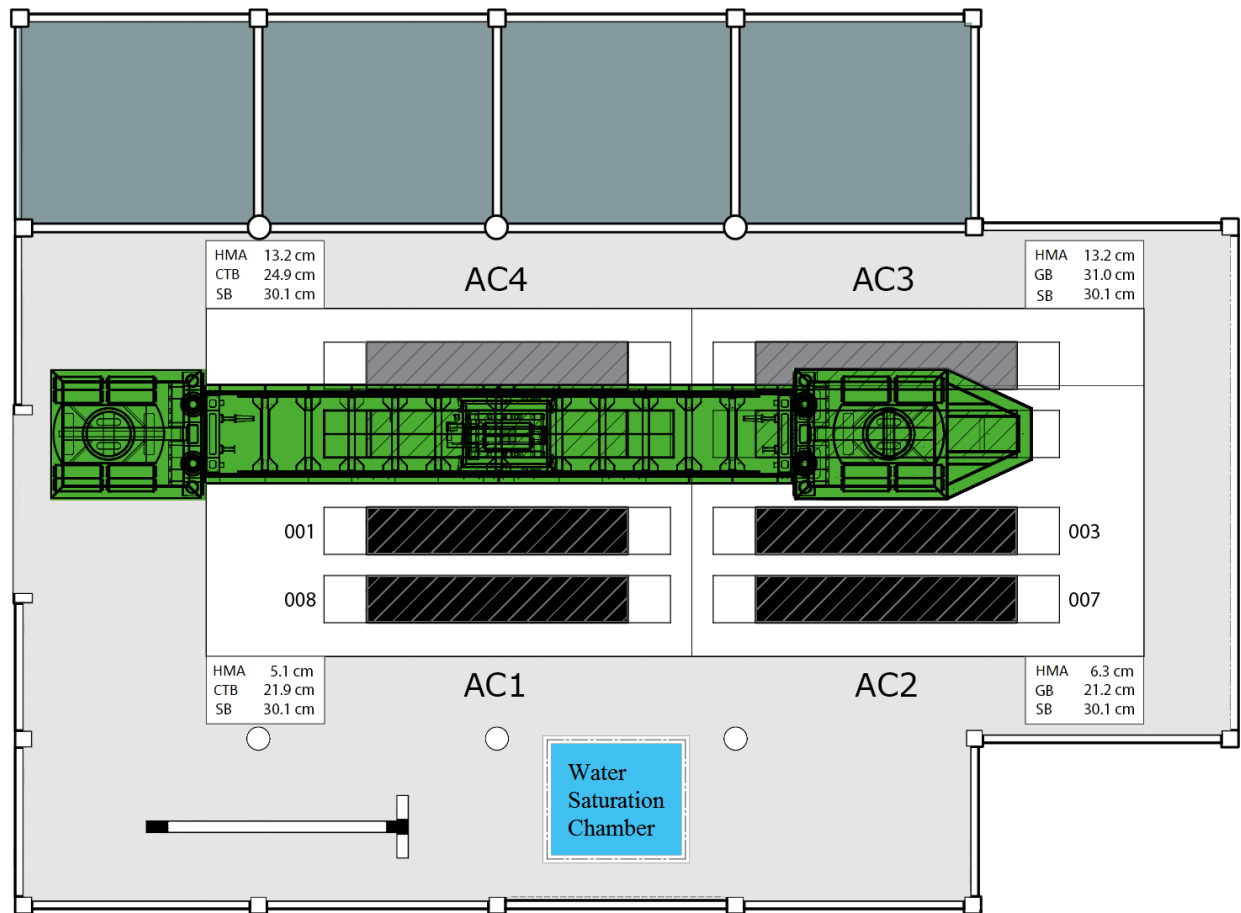
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## 41 PAVELAB TEST SECTIONS

42 The test sections used in the analysis are part of the initial set of experiments performed at  
43 PaveLab in Costa Rica, and correspond to 4 structures (AC1 to AC4) that were constructed in  
44 March 2012 (Figure 1) (3). HVS trafficking on the sections began in July 2013 using a dual  
45 11R22-5 tire, with 90 psi inflation pressure, applying a standardized load between 40 kN and 80  
46 kN. The objective of this set of experiments consisted in the structural comparison of typical

1 conditions in the Central American region: use of granular vs cement-treated bases (CTB), and  
 2 thin vs thick HMA layers. Table 1 summarizes the thickness and material properties of the  
 3 analyzed sections. Layer thicknesses were verified by means of Ground Penetrating Radar (GPR)  
 4 and coring. Initial layer moduli were determined by means of backcalculation based on Falling  
 5 Weight Deflectometer (FWD), Road Surface Deflectometer (RSD) and Multi-depth Deflectometer  
 6 (MDD) results (10).

7 One of the advantages of the Pavelab test track is the ability to change the moisture in the  
 8 pavement layers. to this end; a water saturation chamber was built (Figure 1), which allows to  
 9 generate and control the water table in the test section and therefore, modifying the moisture in the  
 10 pavement layers. In this experiment, the test track numbers 001AC1 and 003AC2 are the dry test  
 11 sections and the 008AC1 and 007AC2 are the saturated ones.  
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13  
 14 **FIGURE 1 Test track distribution.**

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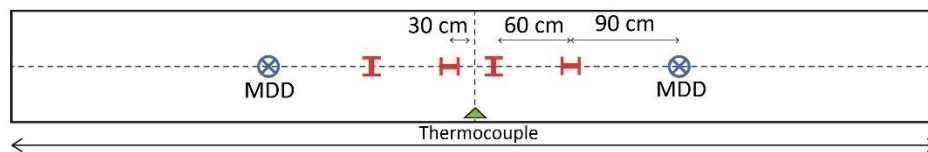
1 **TABLE 1 Test tracks in-place properties after construction.**

Section Properties	001A C1	003AC2	008AC1	007AC2
AC Thickness (H1), cm	6.1	6.3	6.1	6.3
Base Thickness (H2), cm	21.9	21.2	21.9	21.2
Subbase Thickness (H3), cm	30.1	30.1	30.1	30.1
AC Modulus (E1)@25 °C & 1.5 Hz, MPa	3500	3500	3500	3500
Base Modulus (E2), MPa	1200	115	1750	300
Subbase Modulus (E3), MPa	142	75	500	100
Subgrade Modulus (E4), MPa	104	75	60	30

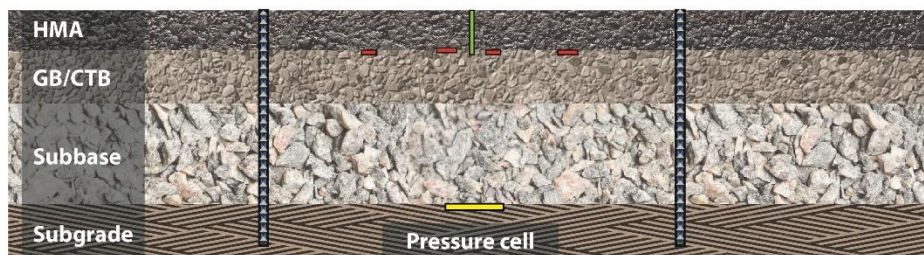
2 **INSTRUMENTATION**

3 The measurements were performed using the HVS integrated instrumentation and embedded  
4 sensors in all four test sections. HVS onboard instrumentation record different signals: the applied  
5 load, tire pressure and temperature, position and velocity of the load carriage. Embedded sensors  
6 included asphalt strain gauges, pressure cells, multi-depth deflectometers (MDDs), and moisture  
7 and temperature probes. The HVS was equipped with a laser profiler that can be used to recreate a  
8 three-dimensional profile of the section. Additionally, a road surface deflectometer (RSD) to  
9 obtain deflection basins at any location along the test section.

10 Figure 2 shows the instrumentation array used for the experiments. The asphalt strain  
11 gauges were placed at the base/HMA layer interface in the longitudinal and transverse directions.  
12 Pressure cells were placed at the subbase/subgrade interface. MDDs were installed at 4 different  
13 depths to cover all 4 structural layers.  
14



Section Length= 6.0 m

15 **FIGURE 2 Sensor array used for each test track.**

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19 Data collection of the 3D profile, strain, pressure, temperature, and deflection was  
20 performed based on load repetitions. At the beginning of each test, data was obtained at short  
21 intervals: 1,000, 2,000, 5,000, and 10,000 loads repetitions. After 20,000 load repetitions, data is  
22 collected on daily basis. Inspection of fatigue and reflective cracking, friction loss, loss of

1 aggregate-asphalt bond, and any other surface deterioration is performed on daily basis during the  
 2 HVS maintenance check.

3 Finally, International Roughness Index (IRI) was calculated by means of a quarter-car  
 4 vehicle math model for each of the longitudinal data lines: the transverse measurements are  
 5 independent. A limitation associated to the IRI estimation is that the length of the section is 6 m,  
 6 and within this distance the effective measuring distance of the lasers is 5.1 m. Therefore, the IRI  
 7 corresponds to an average property within the defined distance.

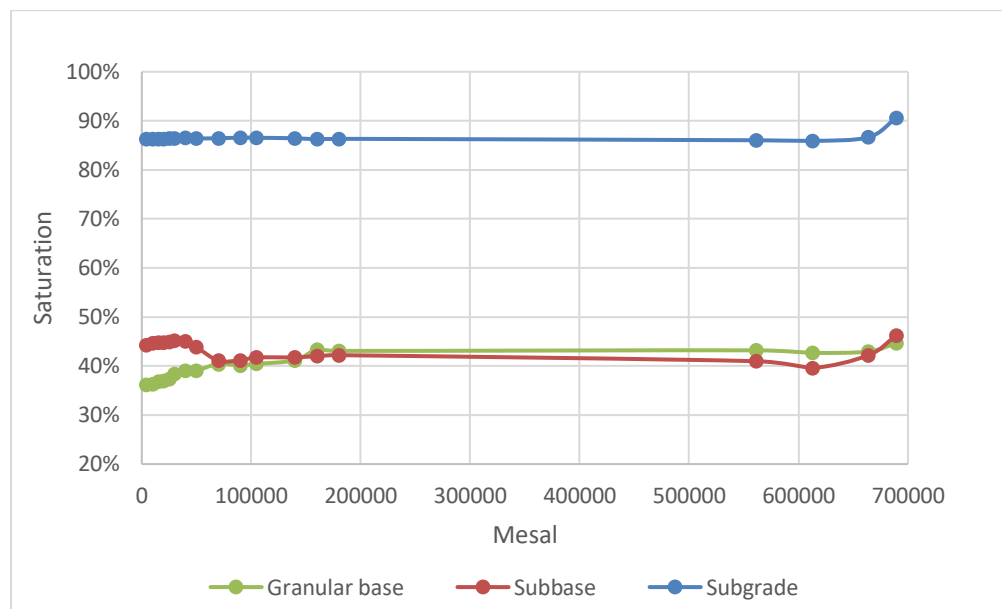
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## 9 SATURATION OF THE TEST TRACKS

10 The humidity levels were strictly controlled, to maintain the constant water table at 70 cm from the  
 11 pavement surface. This water table allows to maintain saturation levels in the subgrade around 87% (Figure  
 12 3), and the optimum dry density of this soil is reached at 80% of saturation (equivalent to an optimum  
 13 humidity of 55%). For the base and subbase layers, the saturation level was established around 43%  
 14 (equivalent to an optimum humidity of 4%) to obtain the optimum density.

15 To control the water table, the saturation chamber has an automated system to ensure the optimal  
 16 flow of water to maintain stable humidity conditions.

17



18

19 **FIGURE 3 Example of controlled moisture conditions on 007AC2 test section.**

## 20 FATIGUE CRACKING

21 Fatigue cracking is one of the most important distresses in flexible pavements. The cracks in  
 22 pavement structures can start from top or at the bottom of the asphalt layer (*II*). In the PaveLab was  
 23 observed that the cracks start at the bottom of the asphalt mixture layer due to the large stresses  
 24 produced by the traffic loads and these propagate as damage increases. Fatigue resistance of the  
 25 asphalt layers depends on the properties of the material and the structural capacity of the  
 26 pavement. In the laboratory, one of the most popular test procedures used to determine  
 27 susceptibility to fatigue cracking is the four point bending beam (4PBB) test, in accordance with  
 28 AASHTO T 321.

29

30 This test is considered to simulate the flexural stresses that an HMA layer experiences in a  
 31 pavement structure. The results are interpreted in terms of a relationship between applied strain or  
 applied stress and the number of cycles to failure. There are several mathematical models used to

1 predict the fatigue life of asphalt mixtures, the simplest being the model proposed by Pell (12). For  
 2 a controlled strain test, the fatigue model is described by Equation 1:

$$3 \quad 4 \quad N_f = k_1 \left( \frac{1}{\varepsilon} \right)^{k_2} \quad (1)$$

5  
 6 Where  $N_f$  = number of cycles to failure,  $\varepsilon$  = tensile microstrain, and  $k_1, k_2$  = mix-dependent  
 7 regression coefficients.

8 The previous approach is a simplified method to analyze the fatigue performance of HMA  
 9 pavements. It is mainly an empirical approach and does not provide a relation between the actual  
 10 load and any form of damage accumulation in the asphalt mixture (13). The obtained results are  
 11 material dependent, loading mode dependent, or both, and consequently this approach can not be  
 12 applied directly to real loading scenarios of in service pavements structures (14). In addition, the  
 13 relationship between fatigue life and stress level is assumed linear, which previous research has  
 14 shown to be inadequate for low strain conditions (15).  
 15

## 16 PROPOSED MODEL

17 Damage functions can be used for modeling cracking of bound materials, permanent deformation,  
 18 and roughness for all layers. The general format of a damage function can be expressed as (16).  
 19

$$20 \quad 21 \quad Damage = A \times MN^\alpha x \left( \frac{resp}{resp_{ref}} \right)^\beta x \left( \frac{E}{E_{ref}} \right)^\gamma x e^{\delta T} \quad (2)$$

22 Where  $MN$  = the number of load repetitions in millions,  $resp$  = the response (stress or strain),  
 23  $resp_{ref}$  = a reference response (can be related to strength),  $E$  = the modulus of the material (adjusted  
 24 for climate and damage),  $E_{ref}$  = a reference modulus, and  $A, \alpha, \beta,$  and  $\gamma$  = model constants.

25 For bound materials, structural damage may be defined as the relative decrease in  
 26 modulus, i.e. the decrease in modulus ( $dE$ ) relative to the initial modulus ( $E_i$ ). During the early  
 27 stages in the life of the layer, the decrease in modulus will primarily be due to microcracking  
 28 which, will later develop into macro-cracking. The process is complex and using the average  
 29 modulus of the layer is a simplification.

## 29 RESULTS

### 30 Four Point Bending Beam (4PBB) Fatigue Tests

31 Tests were performed for laboratory produced and plant asphalt mixes to the number of load  
 32 repetitions required to reach 50% stiffness reduction as function of the tensile strain at different  
 33 temperatures. Tests were conducted in accordance with AASHTO T 321 under constant strain  
 34 loading at three strain levels 400, 600 and 800 microstrain and three test temperatures (10, 20 and  
 35 30 °C) (17).

36 Table 2 shows all the regression coefficients computed for both laboratory and plant  
 37 mixes. In both cases, it was determined that the modulus of the mixture was not statistically  
 38 significant for a 95% confidence level. This could be due to the high correlation (R-value = 0.91)  
 39 between temperature and modulus (collinearity) and the limited number of observations used to  
 40 develop each model.

1 **TABLE 2 Regression estimates for laboratory fatigue models.**

Mix	Coefficient	Value	Std. Error	T-stat.	P-value
Laboratory	A	0.189	0.0079	65.85	<0.05
	$\alpha$	0.271	0.0014	162.82	<0.05
	$\beta$	1.070	0.0084	117.12	<0.05
	$\gamma$	0.535	0.0081	19.23	<0.05
	$\delta$	0.035	0.0005	32.29	<0.05
	Residual Standard Error		0.04897 for 25,172 degrees of freedom		

2  
3 Damage of the asphalt mixture was defined as the relative decrease in modulus  $dE$   
4 relative to the initial modulus,  $E_i$  for each sample and this was used to calibrate the model shown in  
5 Equation 3. The parameters on this equation were determined from 4PBB strain controlled  
6 samples, by minimizing the Root Mean Square (RMS) of the difference between the measured and  
7 the calculated damage from Equation 2 with the incorporation of the temperature variable (17).  
8

$$\omega = A \times (MN)^\alpha \times \left(\frac{\varepsilon}{200}\right)^\beta \times \left(\frac{E}{3000}\right)^\lambda \times e^{(\delta \times T)} \quad (3)$$

9 Where

10 MN = the number of load repetitions in millions

11  $\varepsilon$  = tensile micro strain

12 E = the modulus of the material, MPa

13 T = Temperature °C, and,

14  $\alpha, \beta, \lambda, \delta$  = coefficients from table 2  
15

16 The initial calibration corresponds to apply an adjustment factor of 1.4, to the equation 3.  
17 This factor was generated with preliminary HVS data analyzes of sections with thick layers and  
18 dry conditions and this work was presented in a previous work (17)

### 19 Backcalculated Layer Moduli

20 RSD deflection data was used to determine the progression of the pavement layer moduli through  
21 backcalculation. Figure 4 shows the RSD with the HVS tire. By means of the mentioned  
22 equipment, monitoring the pavement performance under different humidity conditions was  
23 possible. The backcalculation was based on the method of equivalent thickness (MET) where the  
24 thickness of the different layers is transformed into an equivalent single layer. This conversion is  
25 based on Odemark's methodology and the calculation of stresses, strains and deflections was  
26 performed using the Boussinesq theory (18).

27 Damage was determined for the laboratory testing as well as for each individual test  
28 section at five different locations. Three deflection measurements at each location were performed.  
29 Hence, it was possible to determine strain responses based on Layered-Elastic Theory, and these  
30 responses were verified with the strain gauges placed in each track. Also, to determinate the  
31 damage the investigation used temperature records at mid depth of the asphalt layer, thicknesses,  
32 and correspondent load repetitions.

33 Damage on the asphalt concrete was estimated in order to asses how the laboratory model  
34 relates to the APT results. Such estimation was performed using the various coefficients obtained  
35 from laboratory samples (Table 2), The different conditions for each test track indicate that a single



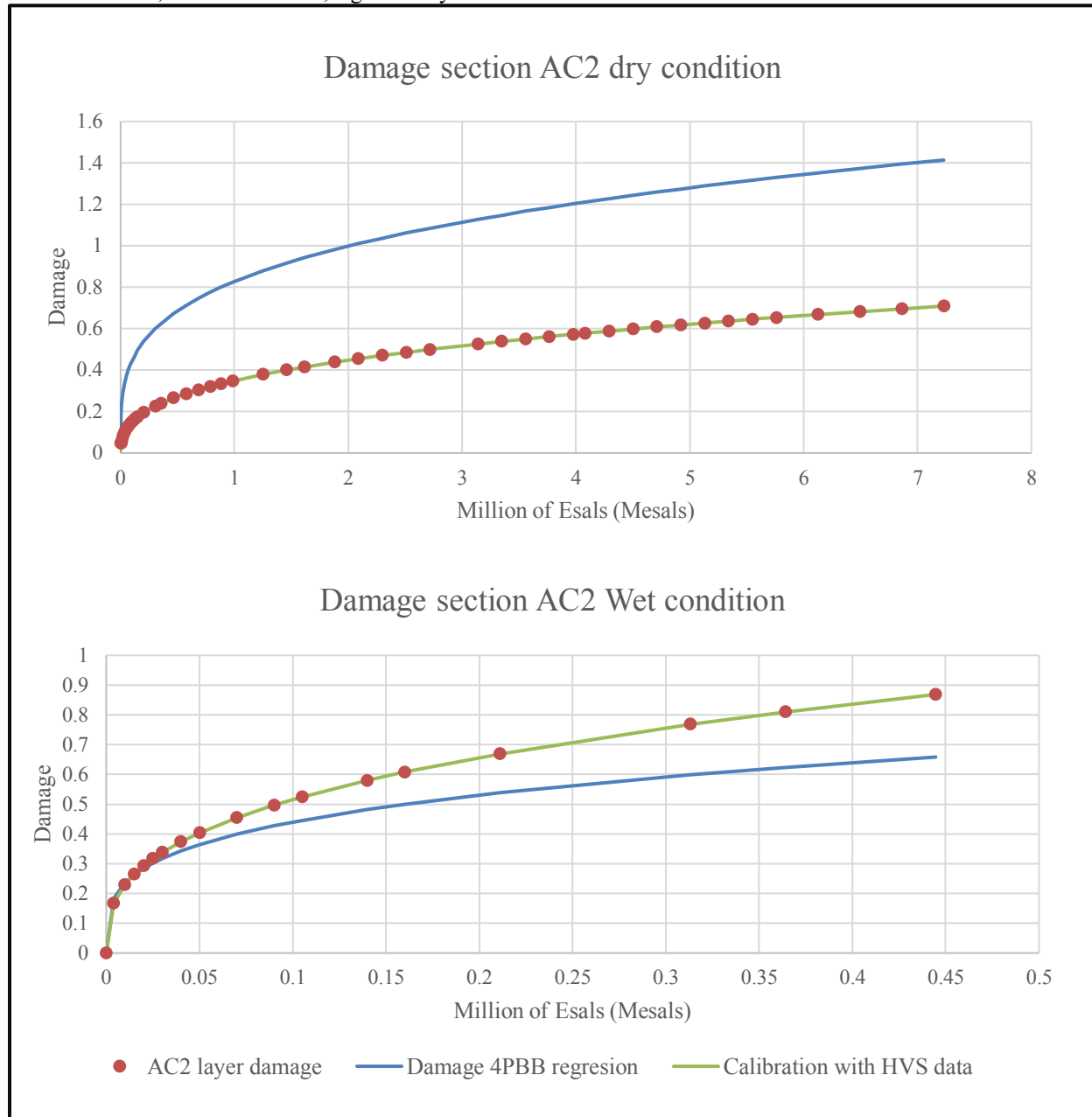
1 adjustment factor might not be adequate in the prediction of fatigue damage. Consequently,  
2 initially independent calibration factors for each test section were developed: granular base, CTB,  
3 optimal humidity or high degree of saturation in the subgrade.



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5 **FIGURE 4 Measurements with RSD equipment and HVS tire.**  
6

7 Figure 5 shows the models calibrated in function of the damage (equation 3) for the AC2  
8 tests tracks (granular base with thin HMA). The calibrated models tend to adequately describe  
9 damage as a function of load repetitions, tensile strain and stiffness, using the parameters initially  
10 determined from 4PBB testing (Table 2).

11 The differences between the laboratory model and the APT test section 003AC2 dry range  
12 between 100% and 150% (Figure 5), respect to the damage observed. This behavior is mainly due  
13 to the measured values of maximum strain at the bottom of the HMA layer used to calibrate the  
14 initial model. For the section 007AC2 wet, the difference between the damage values predicted  
15 from the 4PBB regression and the real measured damage is 6%, however, it has to be considered  
16 that this section fails at 450,000 equivalent axles.  
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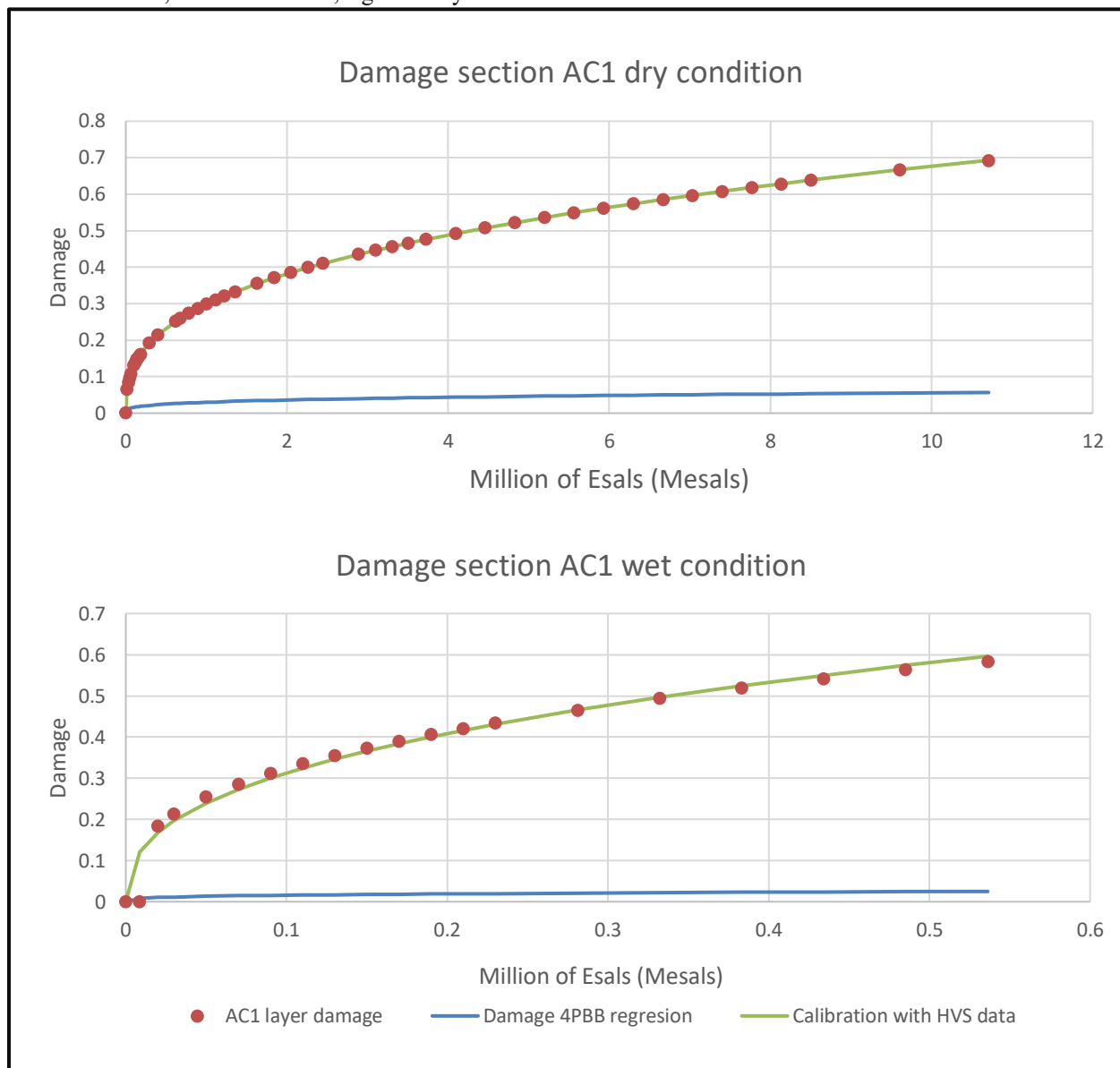


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**FIGURE 5 Predicted damage with HVS data calibration on 003AC2 and 007AC2 sections.**

For the pavements with a CTB layer, the damage predicted with 4PBB regression considerably under-estimates the damage (Figure 6). In this section, the CTB layer causes that the initial strains at the bottom of the HMA layer were very low. These pavement structures had considerably less damage when the experiment was finalized (70% of real damage vs 8% of damage in the 4PBB regression equation).



**FIGURE 6 Predicted damage with HVS data calibration on 001AC1 and 007AC1 sections.**

If the equation 3 is transformed in a classical fatigue function, the model defined in equation 4 is obtained, and the respective calibration coefficients are shown in Tables 3 and 4. The coefficients were calibrated for three damage levels, since for the four test tracks were stopped for damage levels between 60% and 90%. In addition, the models were calibrated for the strain level measured at the bottom of the HMA for each section. In the case of the pavement with CTB the strain was  $15\mu\epsilon$  and in the pavement with granular base was  $353\mu\epsilon$ . It is expected that other test conditions will generate a different model that contemplates other levels of deformation.

$$MN = k_1 * \left(\frac{\epsilon}{200}\right)^{-k_2} * \left(\frac{E}{3000}\right)^{-k_3} \tag{4}$$

Where

$k_1, k_2, k_3$  and  $k_4$ = regression coefficients, corrected with HVS data

1 **TABLE 3 Calibration parameters for thin HMA layer over CTB.**

Section AC1 Dry conditions				Section AC1 Wet conditions			
Coefficients	Damage level			Coefficients	Damage level		
	60%	70%	90%		60%	70%	90%
$k_1$	0.040	0.061	0.124	$K_1$	0.004	0.006	0.012
$k_2$	-3.006			$K_2$	-2.784		
$k_3$	-1.503			$K_3$	-1.392		
$k_4$	-0.099			$K_4$	-0.092		

2 **TABLE 4 Calibration parameters for thin HMA over granular base.**

Section AC2 Dry conditions				Section AC2 Wet conditions			
Coefficients	Damage level			Coefficients	Damage level		
	60%	70%	90%		60%	70%	90%
$K_1$	276.892	425.623	857.887	$K_1$	10.161	15.784	32.365
$K_2$	-2.983			$K_2$	-3.056		
$K_3$	-1.492			$K_3$	-1.528		
$K_4$	-0.098			$K_4$	-0.100		

3

4 **CONCLUSIONS AND RECOMMENDATIONS**

5 The generated fatigue models account for different conditions in terms of materials and humidity  
6 for pavements with a thin HMA layer. Through the present experiment it was verified that the  
7 4PBB regression equation does not fit adequately with the full-accelerated pavement test  
8 performed on HMA thin layer sections.

9 The calibration of the fatigue model coefficients between 4PBB and APT sections showed  
10 in Tables 3 4 are statistically satisfactory for each of the test tracks. Different calibration parameters  
11 were required for each section since the behavior for each test condition was different, mainly for  
12 the test tracks with CTB layer under higher humidity levels.

13 The fatigue models were calibrated for strain levels corresponding to the pavements shown  
14 in Table 1 (AC1 and AC2). Future tests sections will expand the strain level range.

15 Tests currently underway will allow the analysis of the effect of thick HMA layers under  
16 different humidity conditions. The previous will allow for the calibration of a more robust model  
17 based on additional data that consider:

18

- 19 • Universal asphalt concrete fatigue model that predict damage as a function of load  
20 applications, tensile strain and stiffness.
- 21 • Type of base layer (CTB and unbound layers) using parameters from flexural beam testing  
22 (4PBB).
- 23 • Thin and thick HMA layer and humidity on interlayers.

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